# Package: FunSurv (via r-universe)

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Title Modeling Time-to-Event Data with Functional Predictors
Version 1.0.0
<b>Description</b> A collection of methods for modeling time-to-event data using both functional and scalar predictors. It implements functional data analysis techniques for estimation and inference, allowing researchers to assess the impact of functional covariates on survival outcomes, including time-to-single event and recurrent event outcomes.
<b>Depends</b> R (>= $3.5.0$ )
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Contents
ar1_cor AR1_FRAILTY basesurv dar1_cor.drho plot.funsurv simDat

2 AR1\_FRAILTY

ar1\_cor

Construct an AR(1) correlation matrix

# Description

Construct an AR(1) correlation matrix

# Usage

```
ar1_cor(n, rho)
```

# **Arguments**

n number of events for each subject

rho autoregressive correlation

#### Value

A n by n matrix

# **Examples**

```
## Generate AR(1) structure
ar1_cor(n = 5, rho = 0.3)
## first derivative of the AR(1) structure with respect to rho
dar1_cor.drho(n = 5, rho = 0.3)
```

AR1\_FRAILTY

Fit a Functional Regression with AutoregressIve fraiLTY (FRAILTY) model for Recurrent Event Data

## **Description**

Jointly model longitudinal measurements and recurrent events, accommodating both scalar and functional predictors while capturing time-dependent correlations among events. The FRAILTY method employs a two-step estimation procedure. First, functional principal component analysis through conditional expectation (PACE) is applied to extract key temporal features from sparse, irregular longitudinal data. Second, the obtained scores are incorporated into a dynamic recurrent frailty model with an autoregressive structure to account for within-subject correlations across recurrent events. This function works only for univariate functional data.

AR1\_FRAILTY 3

# Usage

```
AR1_FRAILTY(
    formula,
    sdat,
    fdat,
    para0 = c(0.5, 0.5),
    nbasis = 10,
    pve = 0.9,
    npc = NULL,
    makePD = FALSE,
    cov.weight.type = c("none", "counts"),
    iter.max = 50,
    eps = 1e-06
)
```

#### **Arguments**

fdat

nbasis

pve

npc

formula	A formula, with the response on the left of a ~ operator being a Recur object as				
	returned by function Recur in <b>reda</b> , and scalar covariates on the right.				
sdat	A data frame containing subject IDs, time-to-event outcomes (starting time, end				
	point censoring time and event status), and scatar covariates				

point, censoring time and event status), and scalar covariates

A data frame containing subject IDs, longitudinal measurements, and the corresponding time points for each measurement.

para0 A vector of initial values for  $\theta^2$  and auto-regressive coefficient  $\rho$ . Both default to 0.5.

An integer, representing the number of B-spline basis functions used for estimation of the mean function and bivariate smoothing of the covariance surface. Defaults to 10 (cf. fpca.sc in **refund**).

A numeric value between 0 and 1, the proportion of variance explained: used to choose the number of principal components. Defaults to 0.9 (cf. fpca.sc in **refund**).

An integer, giving a prespecified value for the number of principal components. Defaults to NULL. If given, this overrides pve (cf. fpca.sc in **refund**).

makePD Logical: should positive definiteness be enforced for the covariance surface estimate? Defaults to FALSE (cf. fpca.sc in **refund**).

cov.weight.type

The type of weighting used for the smooth covariance estimate. Defaults to "none", i.e. no weighting. Alternatively, "counts" (corresponds to fpca.sc in **refund**) weights the pointwise estimates of the covariance function by the number of observation points.

Maximum number of iterations for both inner iteration and outer iteration. Defaults to 50.

Tolerance criteria for a possible infinite coefficient value. Defaults to 1e-6.

iter.max

eps

4 AR1\_FRAILTY

#### **Details**

## Model specification:

Let  $T_{ij}$  denote the time of the jth event for subject i, and let  $C_i$  represent the censoring time. The observed event time, accounting for right censoring, is  $\widetilde{T}_{ij} = \min(T_{ij}, C_i)$ , and  $\delta_{ij} = I(T_{ij} \leq C_i)$  serves as an indicator of whether the jth event for subject i is observed. The hazard function is specified as

$$h(t; \boldsymbol{Z}_i, X_i(\cdot)) = h_0(t - t_{i,j-1}) \exp(\eta_{ij}),$$

where  $h_0(\cdot)$  is the baseline hazard function, and  $\eta_{ij} = \boldsymbol{\alpha}^\top \boldsymbol{Z}_i + \int_{t_{i,j-1}}^t X_i(s)\beta(s)ds + v_{ij}$ . Here,  $t_{i,j-1}$  is the previous event time with  $t_{i0} = 0$ .  $\boldsymbol{\alpha}$  is the fixed effect parameter associated with the time-invariant covariates  $\boldsymbol{Z}_i$ , and  $\beta(t)$  is a time-varying coefficient that captures the effect of functional predictor  $X_i(t)$  on the hazard rate of recurrent events.

#### Value

A funsury object containing the following components:

beta	Estimation of	of coefficient	s of scalar	covariates and	FPC scores.	Including esti-
Deta	Lammanon	or cocmicicin	s or scarar	covariates and	TIC SCOICS.	including con-

mated values, standard errors, and p-values

beta\_vcov Estimated variance-covariance of the estimates of beta

eAR Estimation of variance components ( $\theta^2$  and  $\rho$ )
eAR\_vcov Estimated variance of estimates of  $\theta^2$  and  $\rho$ frailties Estimated frailty terms (random effects)
basesurv Estimated baseline survival probability

time Time points associated with baseline survival probability

FPC Functional principal components

# See Also

Recur

**PACE** 

#### **Examples**

basesurv 5

basesurv

A function to obtain the baseline survival function

# Description

A function to obtain the baseline survival function

## Usage

```
basesurv(object)
```

# **Arguments**

object

A funsury object

#### Value

A data frame including time and baseline survival

# **Examples**

dar1\_cor.drho

First derivative of AR(1) correlation matrix with respect to the autoregressive coefficient

# **Description**

First derivative of AR(1) correlation matrix with respect to the auto-regressive coefficient

# Usage

```
dar1_cor.drho(n, rho)
```

# **Arguments**

n number of events for each subject rho autoregressive correlation

## Value

A n by n inverse matrix

6 simDat

plot.funsurv

Plot method for 'funsury' objects

#### **Description**

Plot method for 'funsurv' objects

# Usage

```
## S3 method for class 'funsurv'
plot(x, what = c("beta", "fpc", "basesurv"), ...)
```

# **Arguments**

X

A funsury object

what

A character string specifying what to be plotted. Use what = "beta" to plot the estimated  $\beta(t)$ . Use what = "fpc" to plot the functional principal components associated with the the longitudinal measurements. Use what = "basesurv" to plot the baseline survival probabilities.

additional graphical parameters to be passed to methods.

#### Value

A ggplot object ...

#### **Examples**

simDat

Simulated datasets for demonstration

## Description

The dataset was generated based on the proposed model  $h(t; \mathbf{Z}_i, X_i(\cdot)) = h_0(t - t_{i,j-1}) \exp{(\eta_{ij})}$ , where  $h_0(\cdot)$  is the baseline hazard function generated from a Weibull distribution.  $\eta_{ij} = \boldsymbol{\alpha}^{\top} \mathbf{Z}_i + \int_{t_{i,j-1}}^t X_i(s)\beta(s)ds + v_{ij}$ .  $\boldsymbol{\alpha}$  is the fixed effect parameter associated with the time-invariant covariates  $\mathbf{Z}_i$ , and  $\beta(t)$  is a time-varying coefficient that captures the effect of functional predictor  $X_i(t)$  on the hazard rate of recurrent events. The simulated dataset is organized into two data frames: a survival data frame (sdat) and a functional data frame (fdat). The variables in each data frame are listed below:

simDat 7

# Usage

data(simDat)

#### **Format**

A list with two data frame:

**sdat** Survival data; a data frame with xxx rows and xxx variables:

id Subjects identification

event A sequence of the number of events per subject

t\_start Event starting time

**t\_end** Event end time

censoring\_time Event censoring time

status Event status: status=1 if event is observed and status=0 if event is censored

**z1** A univariate scalar covariates. Can be extended to multiple scalar covariates

fdat Functional data; a data frame with xxx rows and xxx variables:

id Subjects identification

time Time points for each longitudinal measurement

x Longitudinal measurements at distinct time points

## Source

Simulated data